

Quantum Numbers

Quantum Numbers

each orbital is characterized by a unique set of quantum numbers

principal quantum number: n

angular momentum quantum number: l
(azimuthal)

magnetic quantum number: m_l

Principal quantum number: n

related to **size and energy** of orbital shells: integral values: 1, 2, 3, ...

higher n

the electron, on average, is farther from nucleus

the electron less strongly bound by nucleus
(higher energy potential)

Angular momentum quantum number: l

related to **shape** of orbital

subshells:

integral values: $0, 1, 2, \dots, n - 1$

$l = 0$: s orbital $l = 2$: d orbital

$l = 1$: p orbital $l = 3$: f orbital

Relation of n and l

$n = 1$	$l = 0$	1s
$n = 2$	$l = 0, 1$	2s, 2p
$n = 3$	$l = 0, 1, 2$	3s, 3p, 3d
$n = 4$	$l = 0, 1, 2, 3$	4s, 4p, 4d, 4f

Magnetic quantum number: m_l

related to orientation of orbital in space

integral values between l and $-l$

Atomic Orbitals

Relation of l and m_l

$$s: l = 0$$

$$m_l = 0$$

$$p: l = 1$$

$$m_l = -1, 0, 1$$

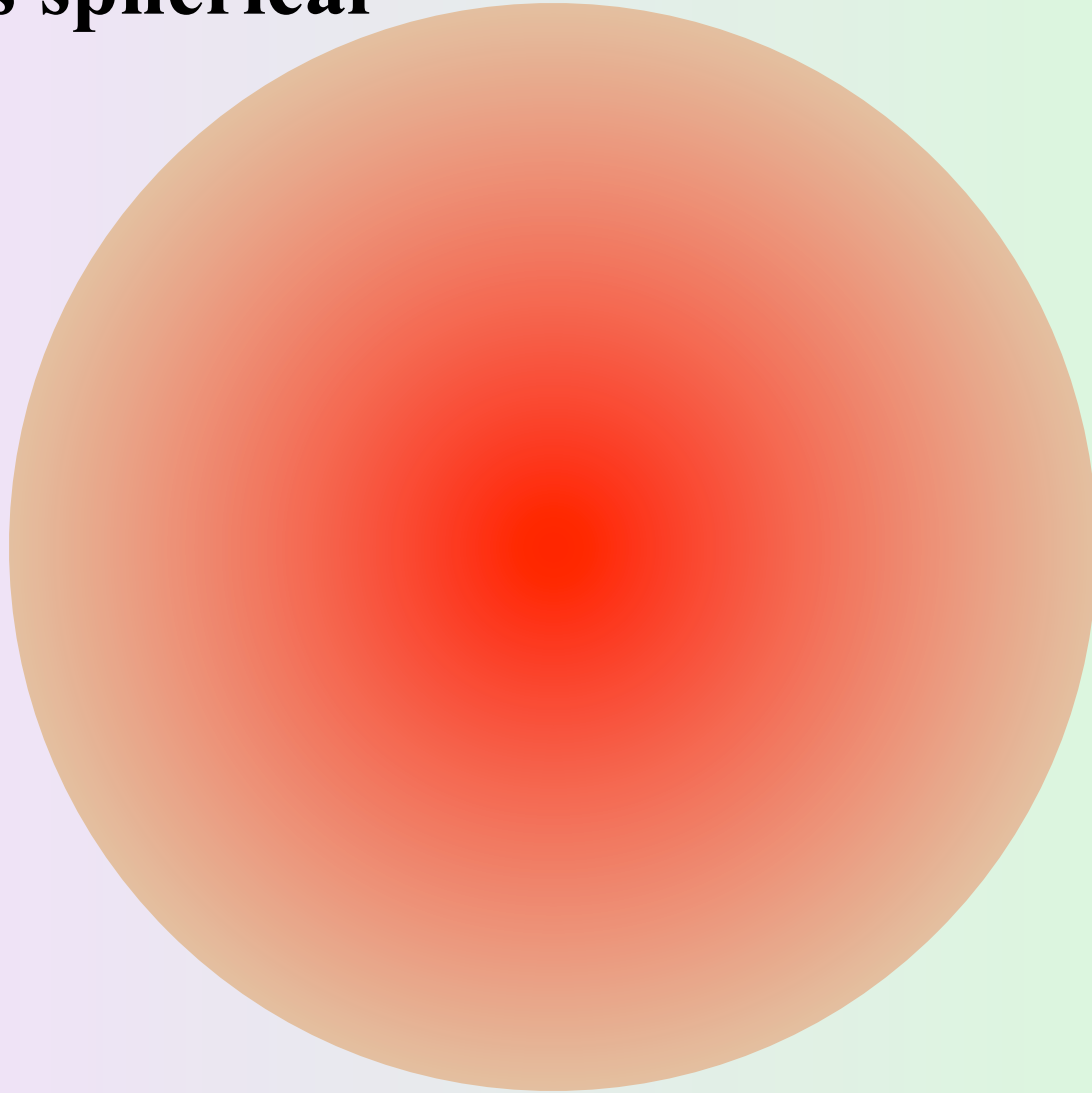
$$d: l = 2$$

$$m_l = -2, -1, 0, 1, 2$$

$$f: l = 3$$

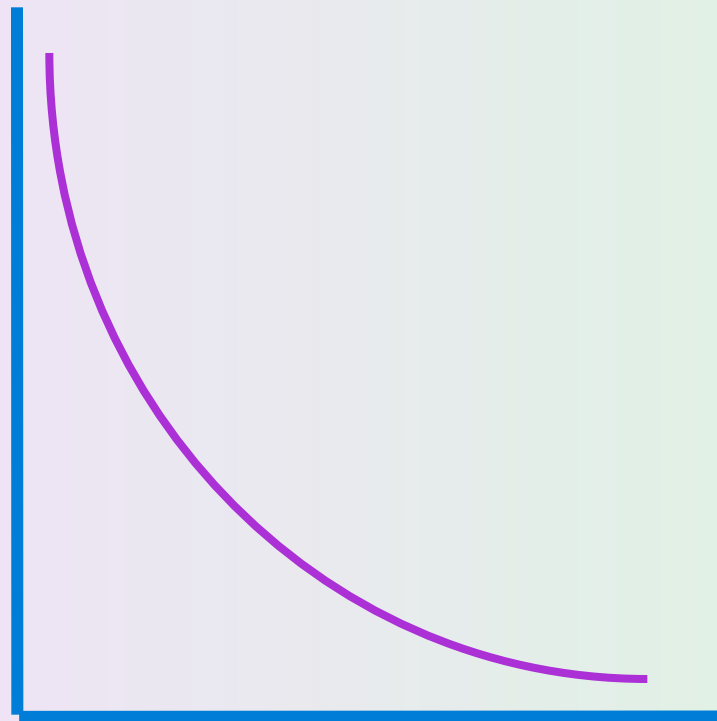
$$m_l = -3, -2, -1, 0, 1, 2, 3$$

Probability distribution for an electron in a 1s orbital is spherical



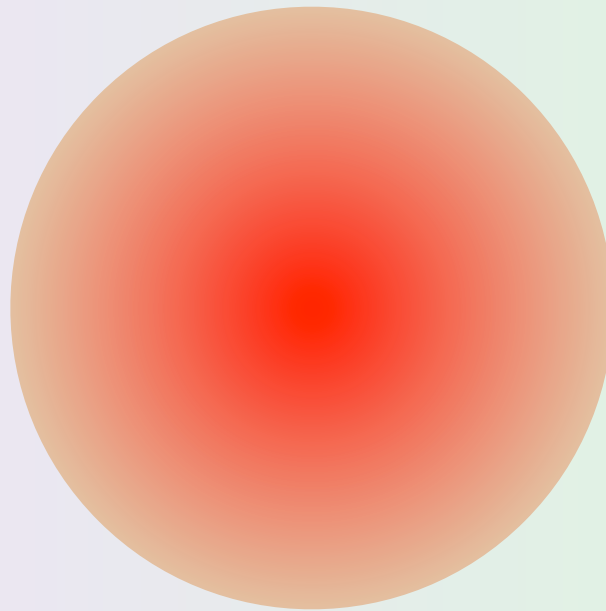
Probability of finding an electron in a 1s orbital at a certain distance on a line originating at the nucleus

Electron density



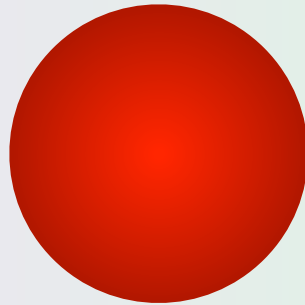
Distance from nucleus

Boundary surface encloses 90% of the total electron probability

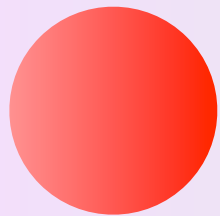


Boundary surface encloses 90% of the total electron probability

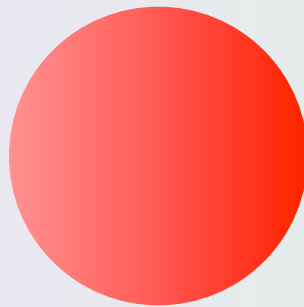
Chemists approximate an orbital by the volume enclosed by the boundary surface



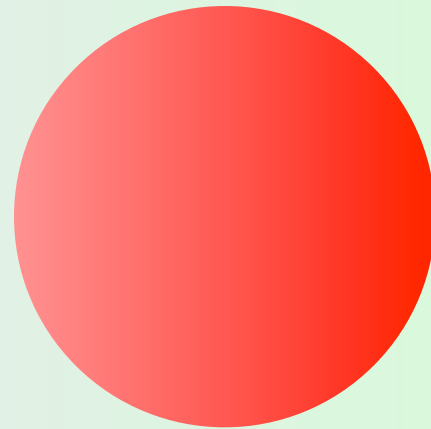
s orbital boundary surfaces



1s

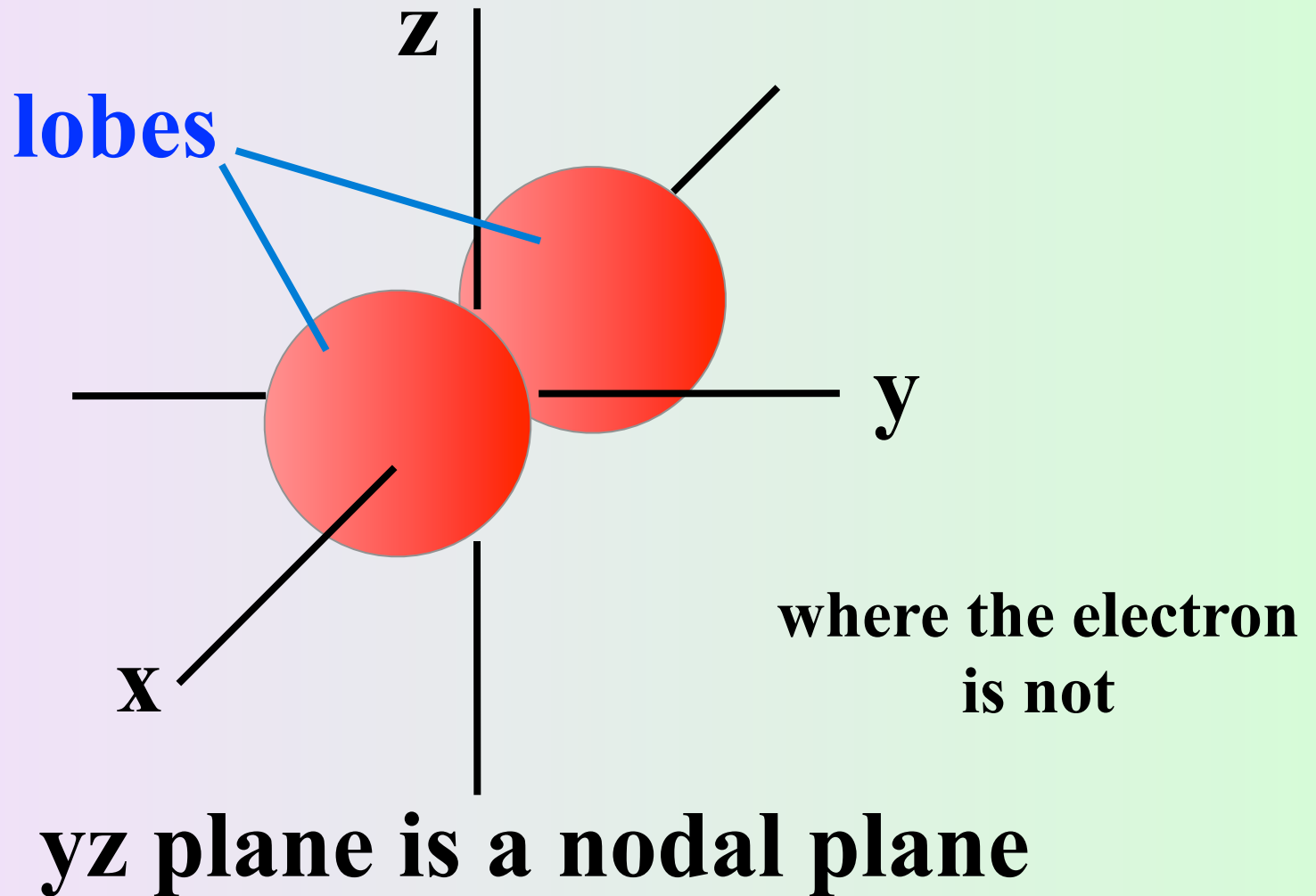


2s

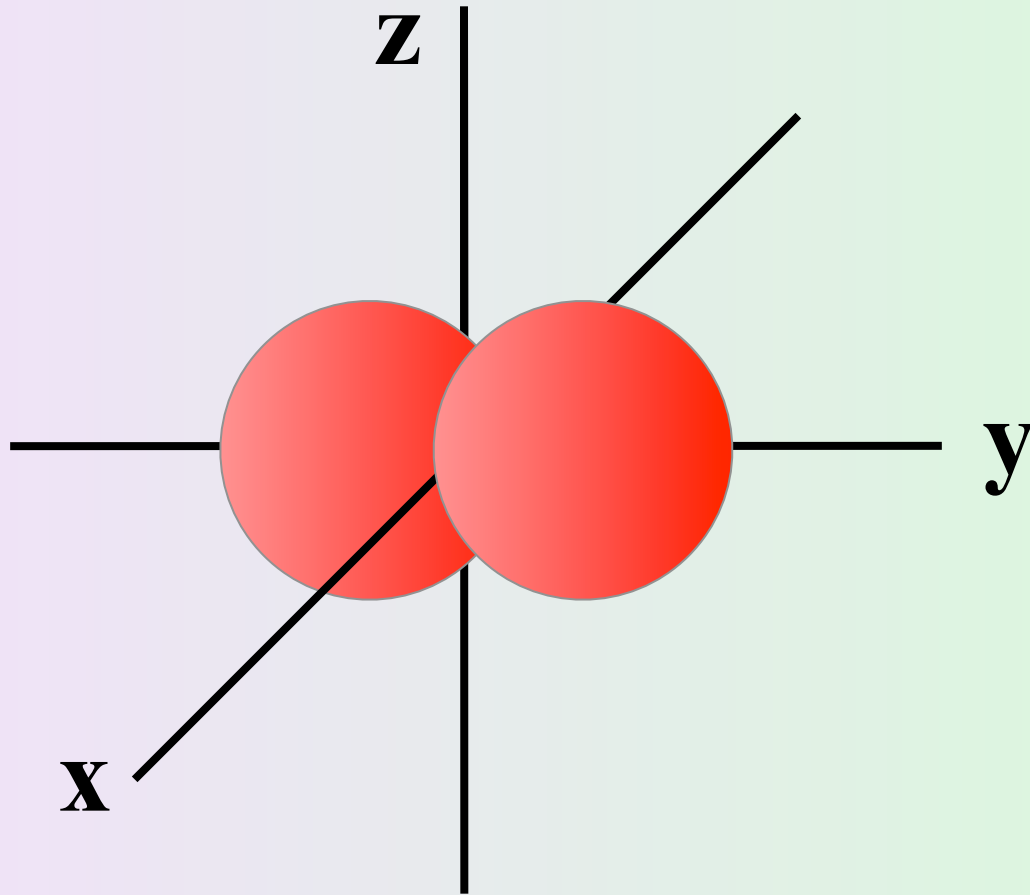


3s

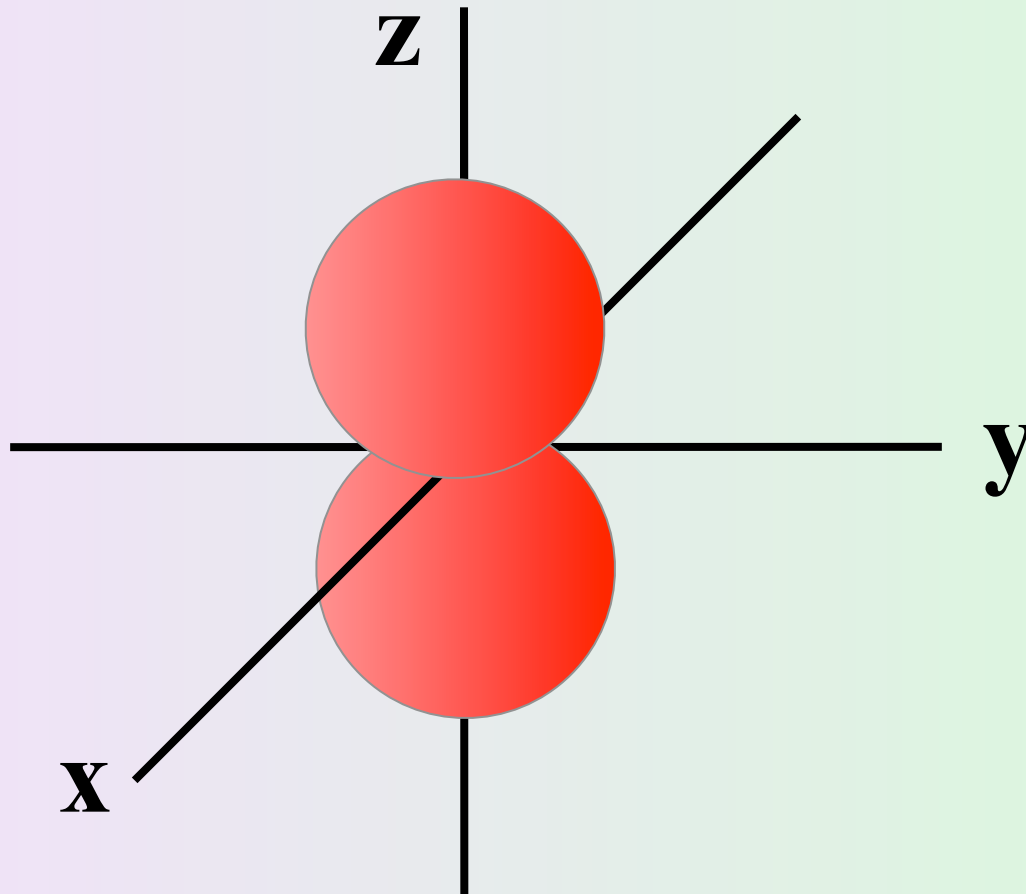
$2p_x$ orbital boundary surface



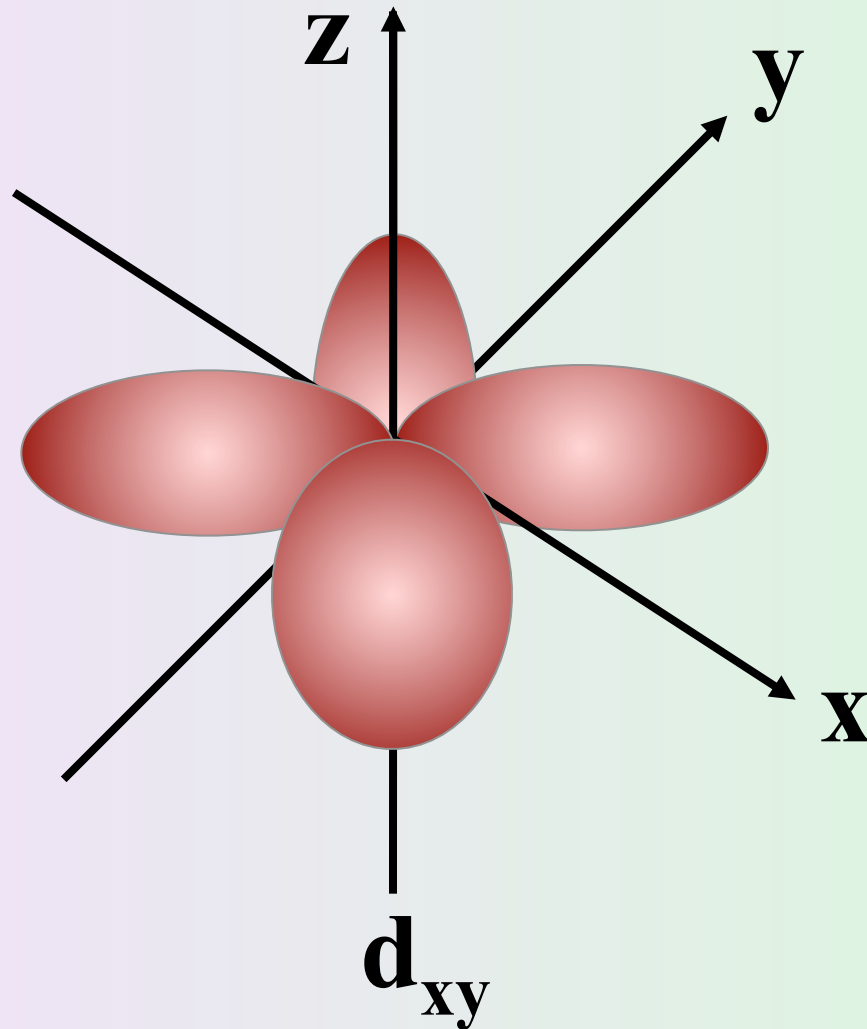
$2p_y$ orbital boundary surface



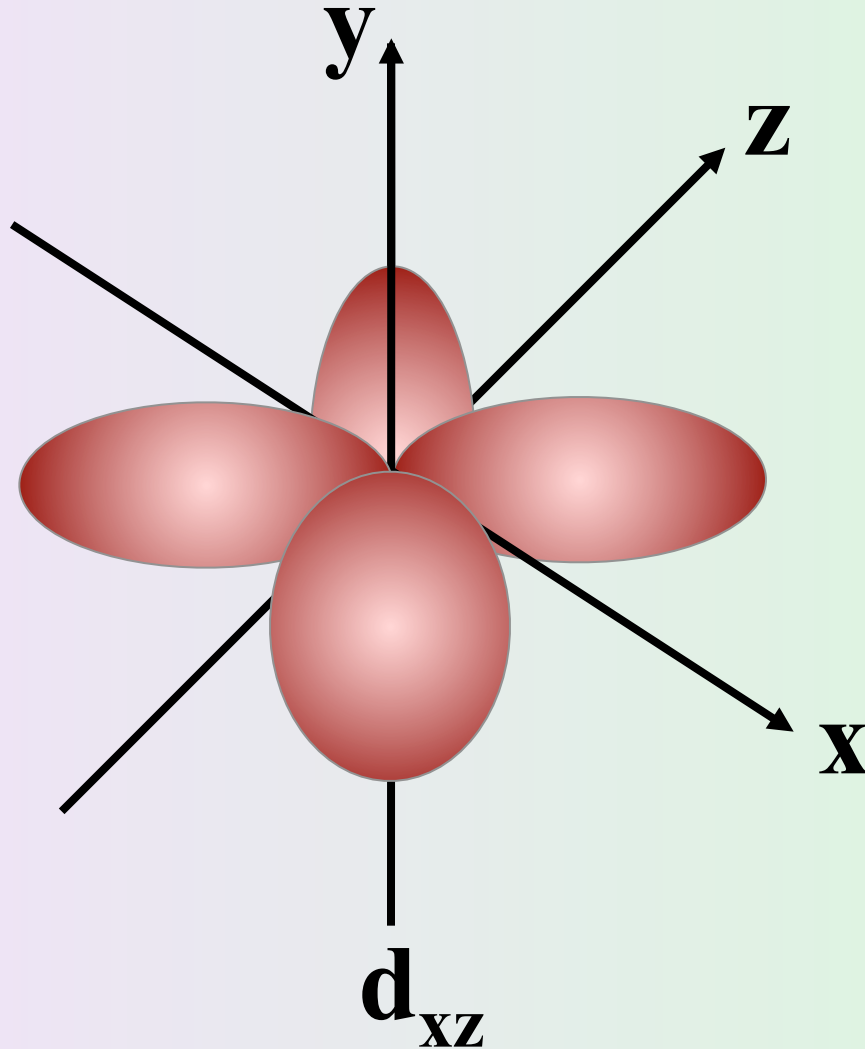
$2p_z$ orbital boundary surface



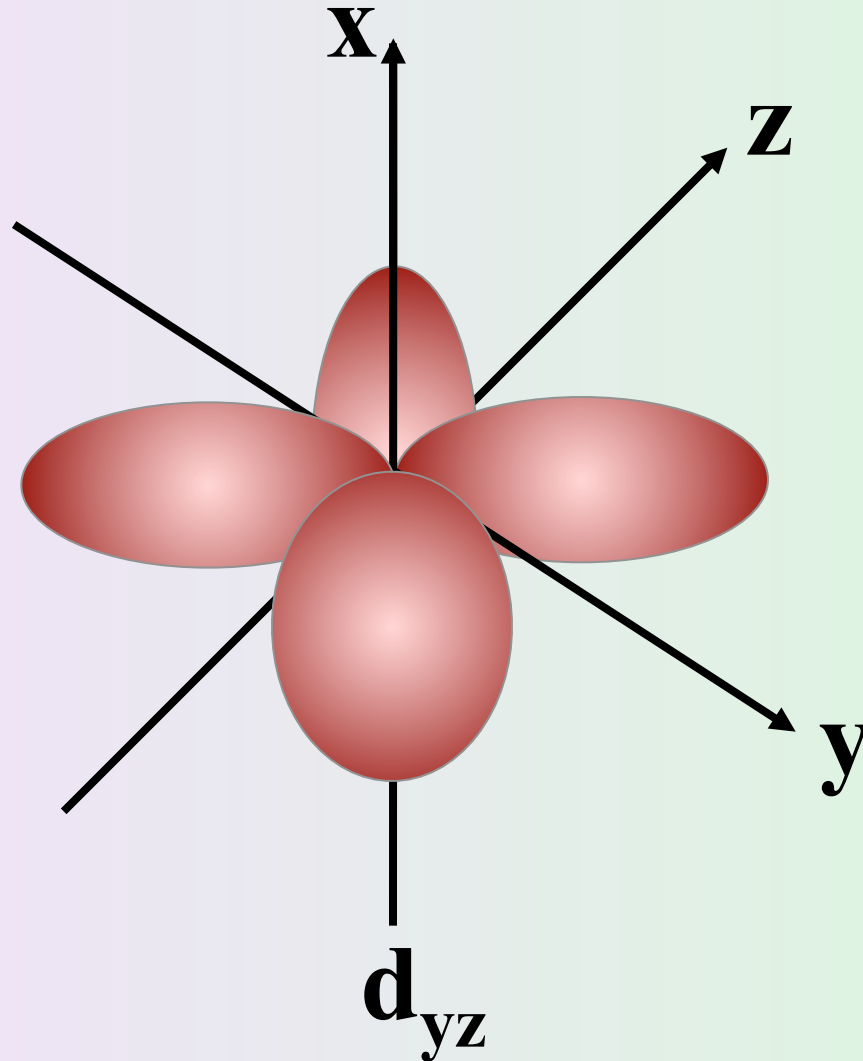
$3d_{xy}$ orbital boundary surface



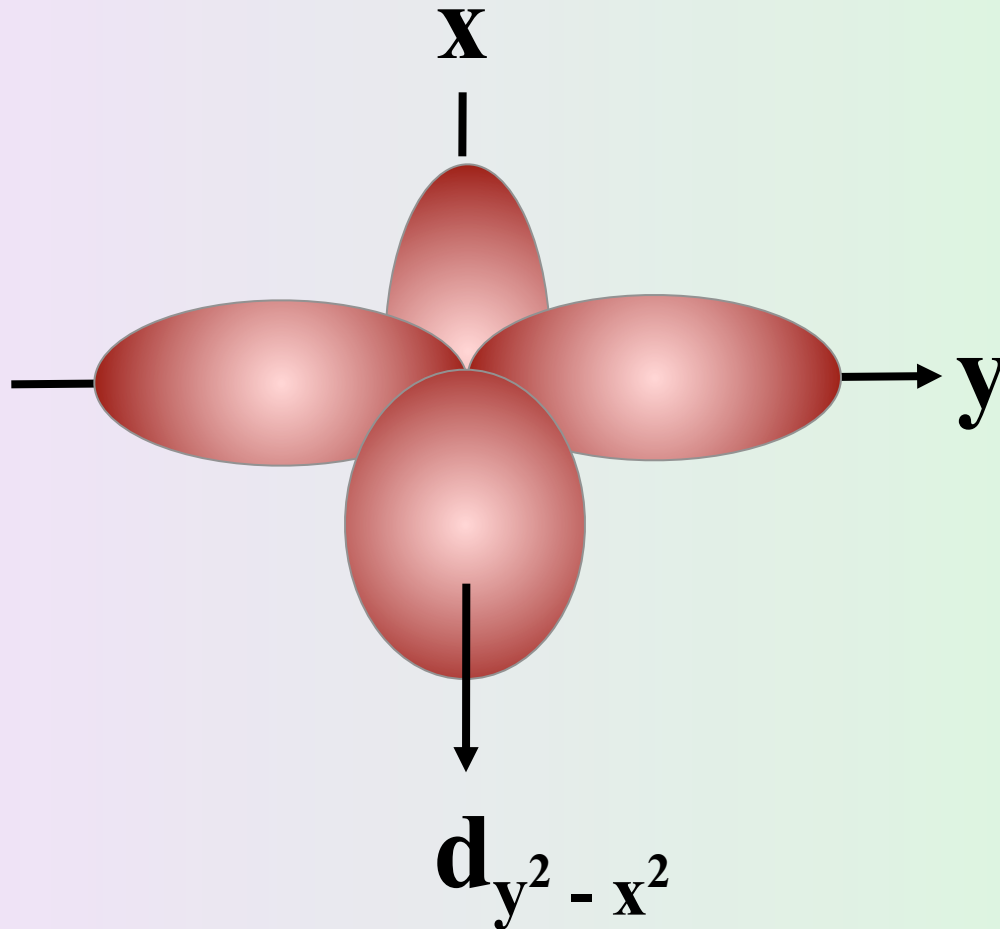
$3d_{xz}$ orbital boundary surface



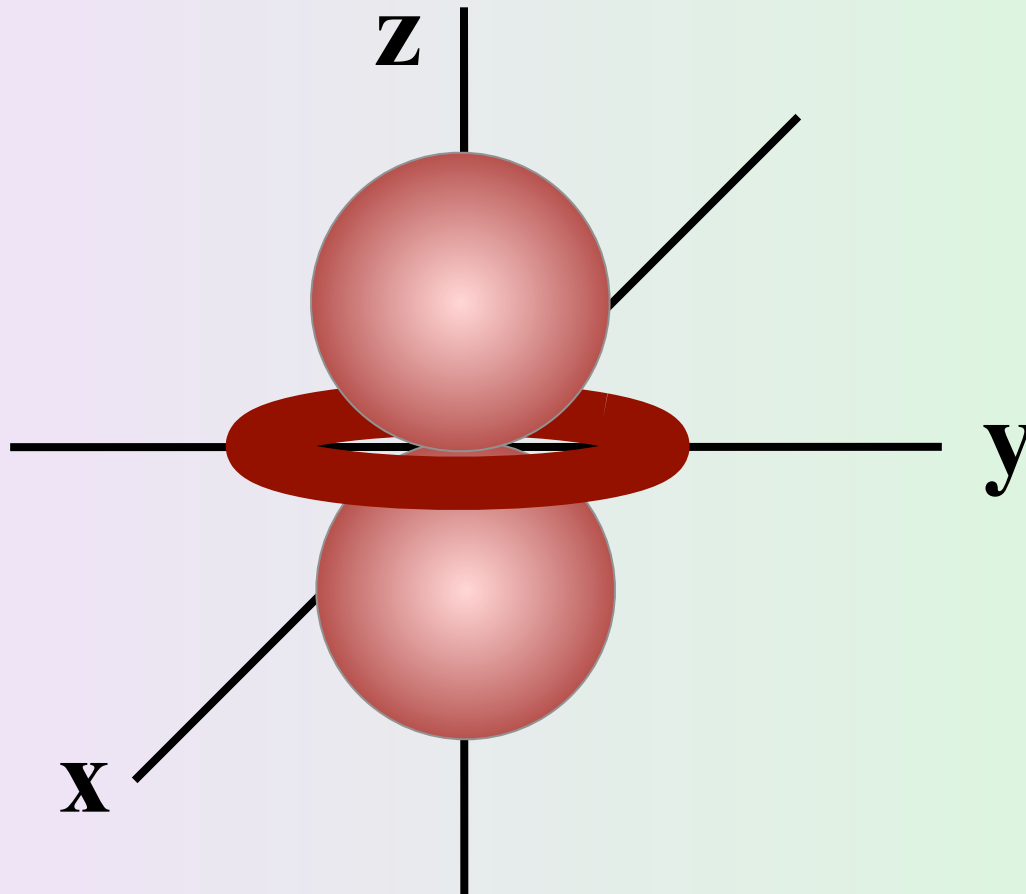
$3d_{yz}$ orbital boundary surface

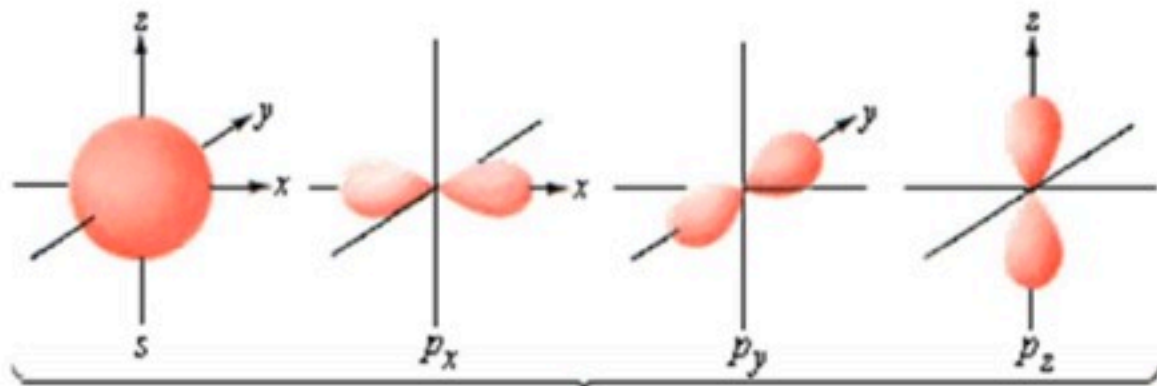


$3d_{y^2 - x^2}$ orbital boundary surface

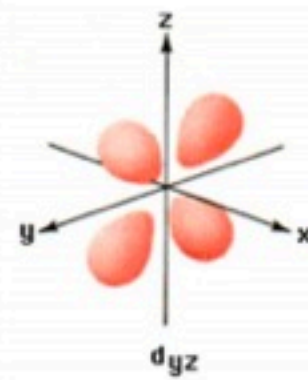
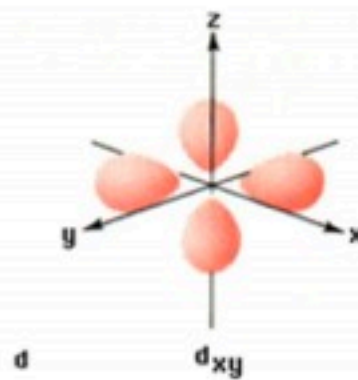
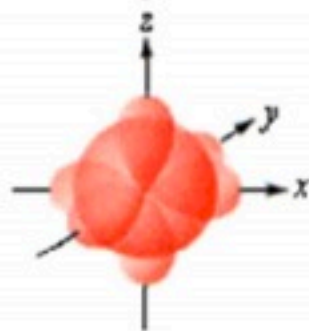


$3d_{z^2}$ orbital boundary surface

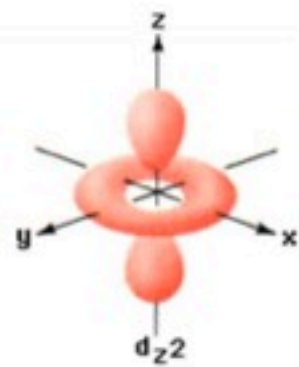
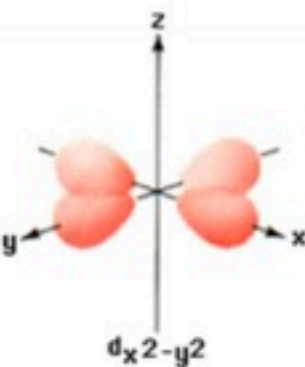
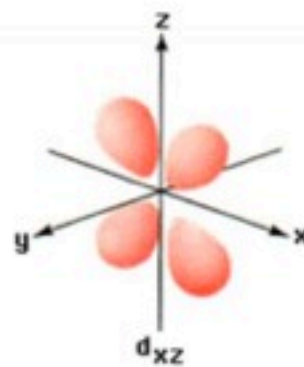




s and p sublevels

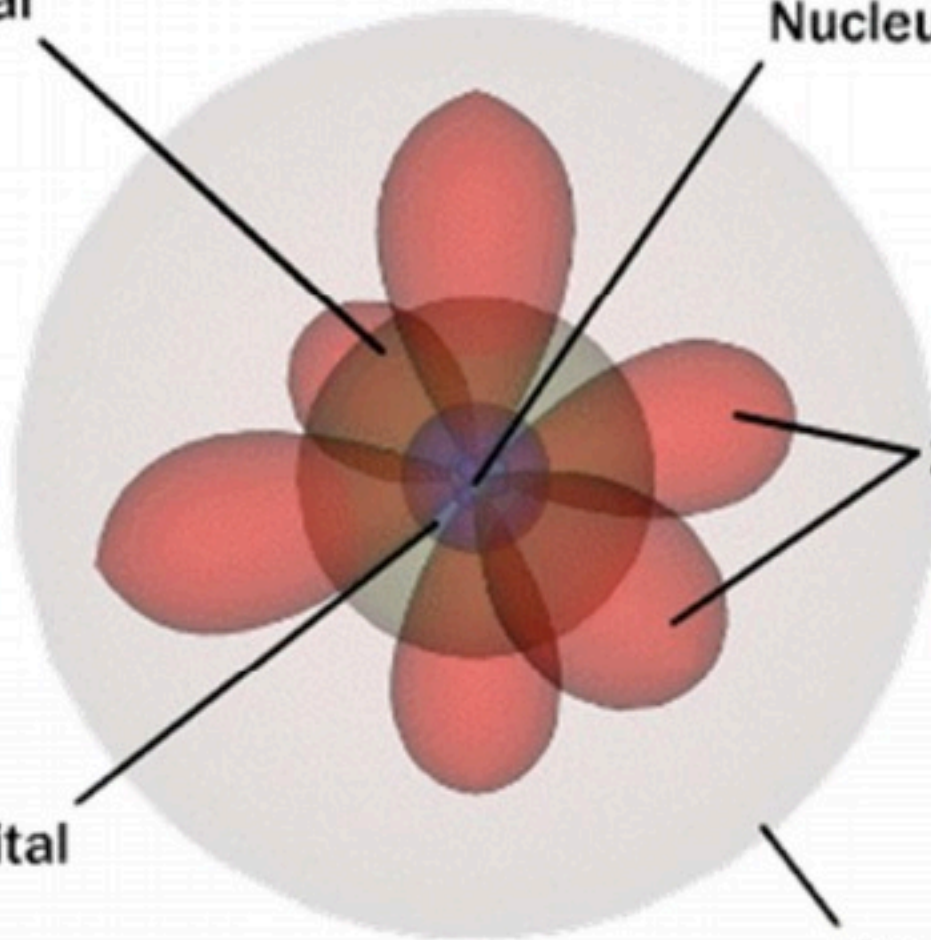


d sublevels



2s orbital

Nucleus



2p orbitals

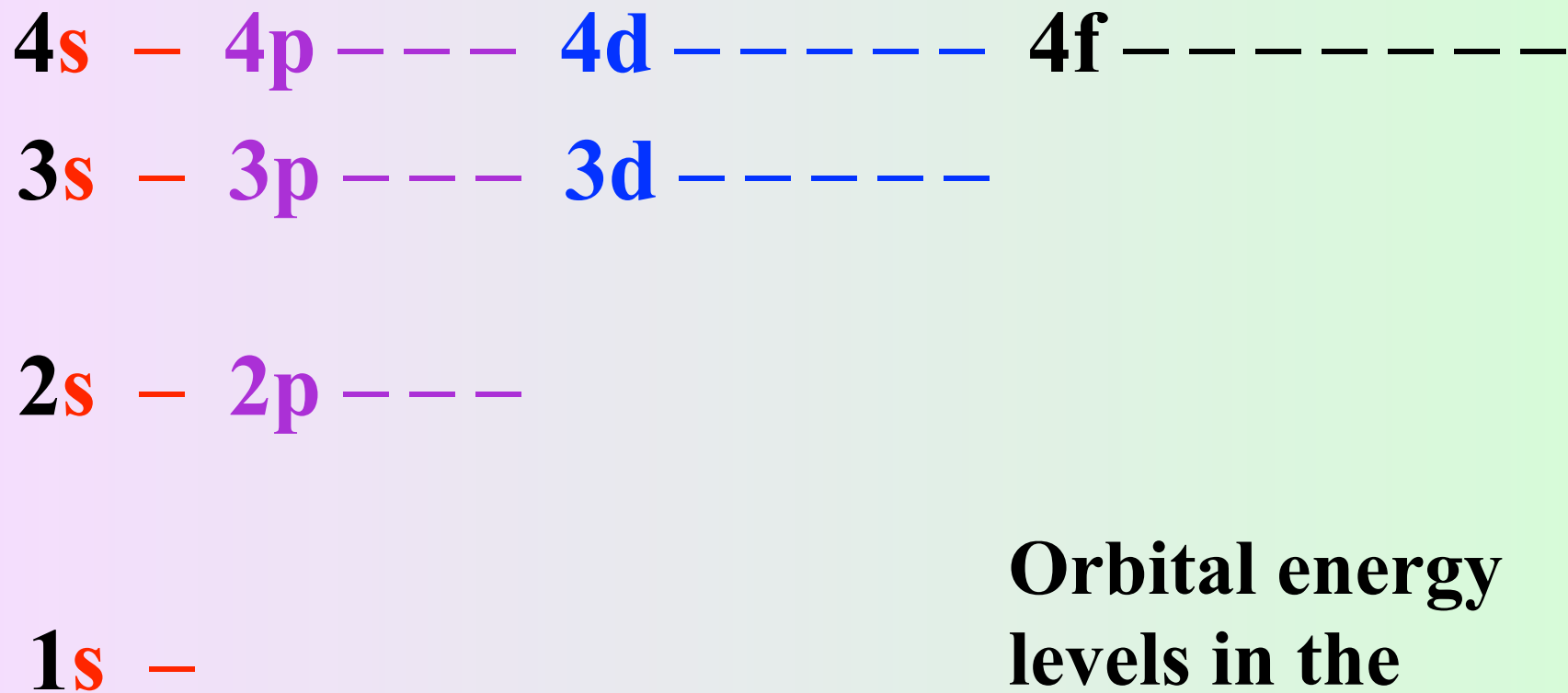
1s orbital

3s orbital

energies of hydrogen orbitals

for the hydrogen atom, all orbitals with the same principal quantum number have the same energy

i.e., they are “degenerate”

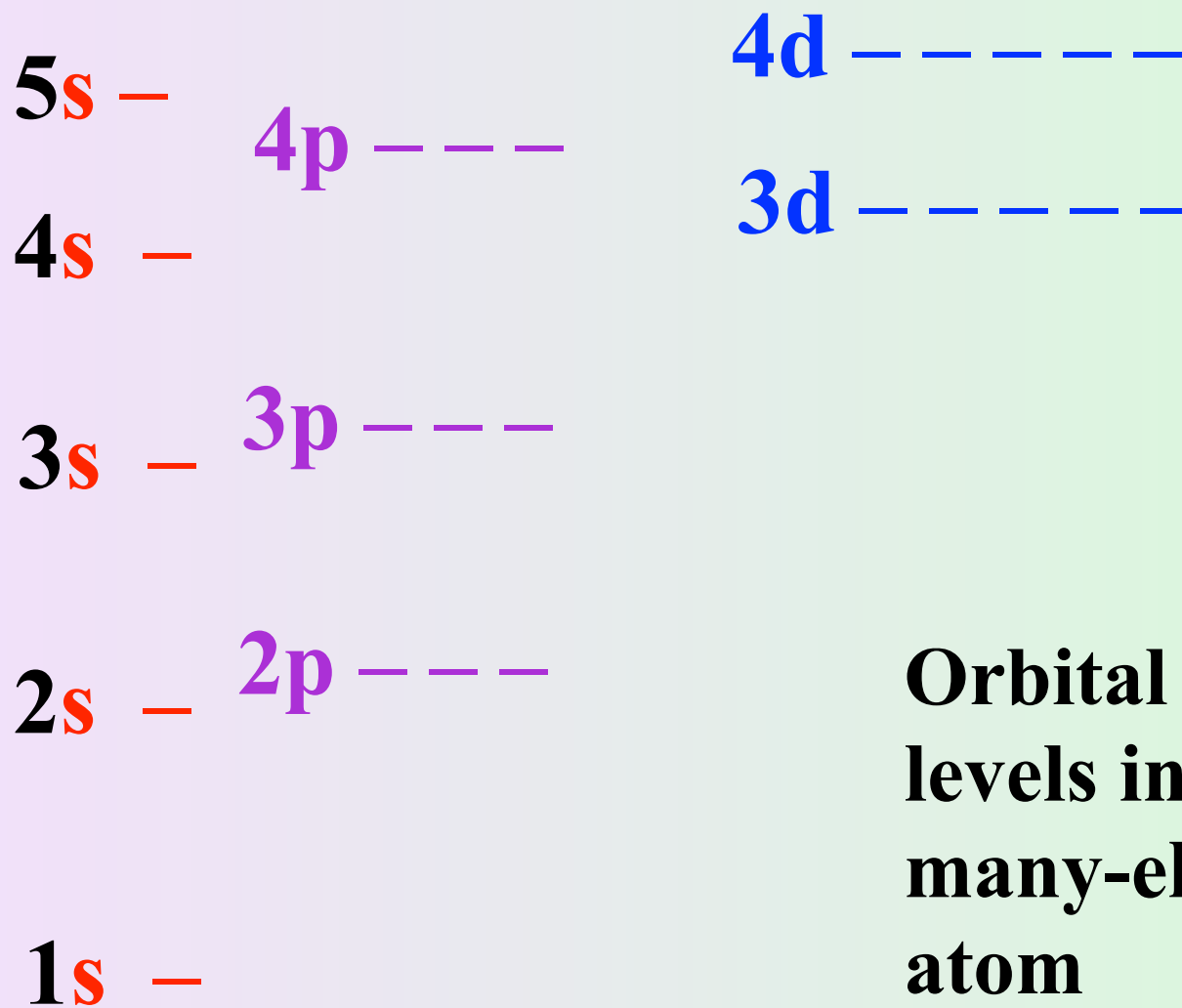


**Orbital energy
 levels in the
 hydrogen atom**

energies of multi-electron orbitals

for a many-electron atom, the energy depends on both the principal quantum number and the angular momentum quantum number

i.e., each subshell represents a different energy in a multi-electron system



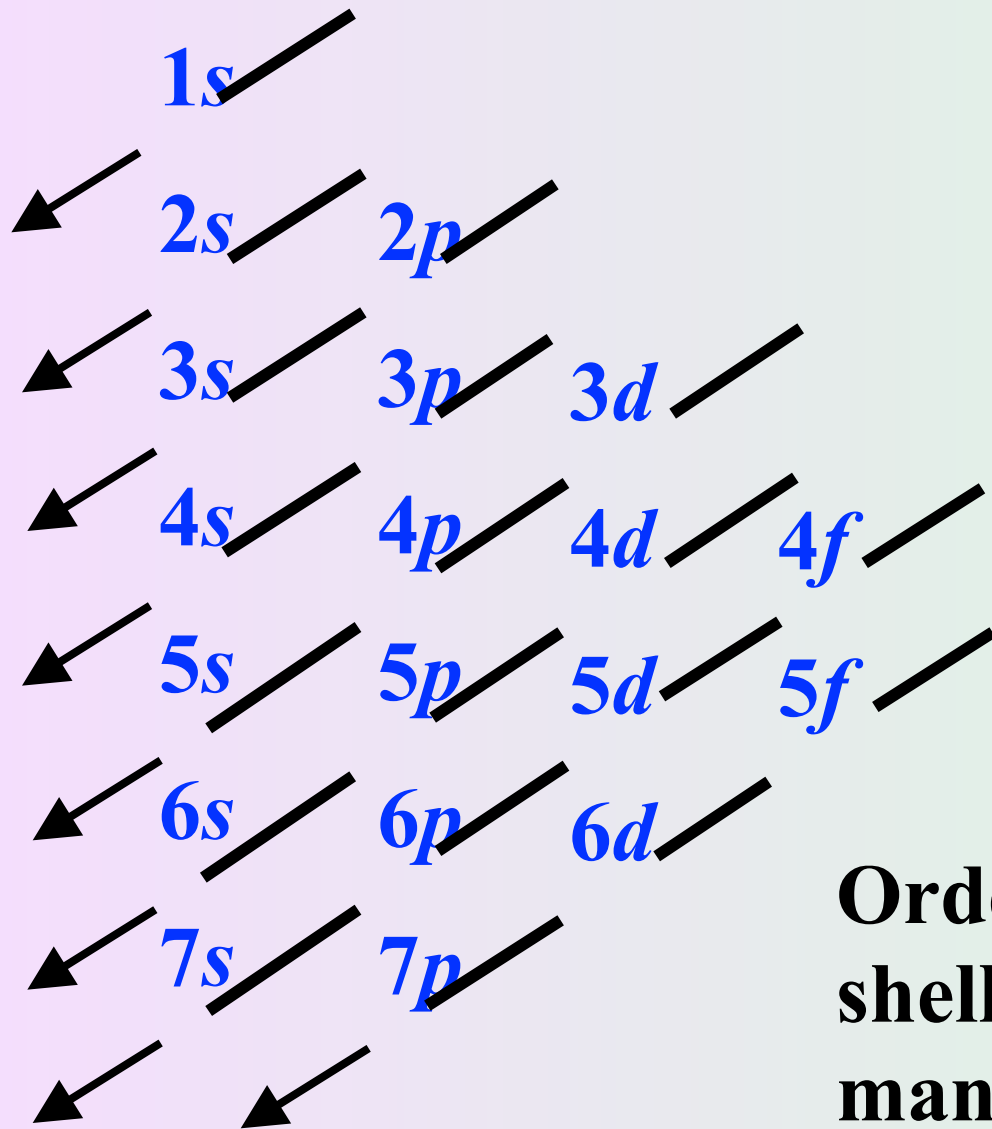
**Orbital energy
levels in a
many-electron
atom**

Shielding Effect

in a many-electron atom, electrons in the $1s$ orbital shield the electrons located in the $2s$ and $2p$ orbitals from the electrostatic attraction of the protons in the nucleus

$2s$ electron density is greater near the nucleus than $2p$ electron density

$2s$ orbital is said to be more “penetrating” and is less shielded than the $2p$



Order in which subshells are filled in a many-electron atom