

Measurement

International System of Units (SI)

- revised metric system proposed in 1960
- widely used in science
- 7 base units

SI Base Units

Length	Meter	m
Mass	Kilogram	kg
Time	Second	s
Electrical current	Ampere	A
Temperature	Kelvin	K
Amount of Substance	Mole	mol
Luminous intensity	Candela	cd

SI Prefixes

Tera-	T	10^{12}	Deci-	d	10^{-1}
Giga-	G	10^9	Centi-	c	10^{-2}
Mega-	M	10^6	Milli-	m	10^{-3}
Kilo-	k	10^3	Micro-	μ	10^{-6}
			Nano-	n	10^{-9}
			Pico-	p	10^{-12}

Derived units in SI

measured in terms of one or more base units

volume

$$\text{m} \times \text{m} \times \text{m} = \boxed{\text{(m}^3\text{)}} = 1000 \text{ (dm}^3\text{)}$$

$$\boxed{1 \text{ dm}^3 = 1 \text{ liter (L)}}$$

density

$$\text{mass/volume} = \boxed{\text{(kg/dm}^3\text{)}} = \text{(g/cm}^3\text{)} = \boxed{\text{(g/ml)}}$$

Density

The mass of a substance that occupies one unit of volume

$$\text{Density} = \frac{\text{mass}}{\text{volume}} = \frac{\text{kg}}{\text{dm}^3} = \frac{\text{g}}{\text{cm}^3} = \frac{\text{g}}{\text{ml}}$$

Example

What is the density of a piece of concrete that has a mass of 8.76 g and a volume of 3.07 cm³

$$\text{Density} = \frac{\text{mass}}{\text{volume}} = \frac{8.76\text{g}}{3.07 \text{ cm}^3} = 2.85\text{g/cm}^3$$

practice problem 1

A piece of metal with a mass of 147 g is placed in a graduated cylinder. The water level rises from 20 ml to 41 ml. what is the density of the metal.

$$41 \text{ ml} - 20 \text{ ml} = 21 \text{ ml}$$

$$\text{Density} = \frac{\text{mass}}{\text{volume}} = \frac{146 \text{ g}}{21 \text{ ml}} = 6.95 \text{ g/ml}$$

practice problem 2

What is the volume of a sample that has a mass of 20 g and a density of 4 g/ml

$$\cancel{20 \text{ g}} \times \frac{\text{ml}}{\cancel{4 \text{ g}}} = 5 \text{ ml}$$

Practice problem 3

A metal cube has a mass of 20 g and a volume of 5 cm³. Is the cube made of pure aluminum?

$$\text{Density} = \frac{\text{mass}}{\text{volume}} = \frac{20 \text{ g}}{5 \text{ cm}^3} = 4 \text{ g/ml}$$

density of Aluminum is 2.7 g/ml

Temperature

There are three systems for measuring temperature that are widely used:

Kelvin scale

$$\mathbf{K = C^{\circ} + 273.15}$$

Celsius scale

$$\mathbf{C^{\circ} = K - 273.15}$$

Fahrenheit scale

$$\mathbf{F^{\circ} = C^{\circ} (9/5) + 32}$$

**Used mainly in
engineering**

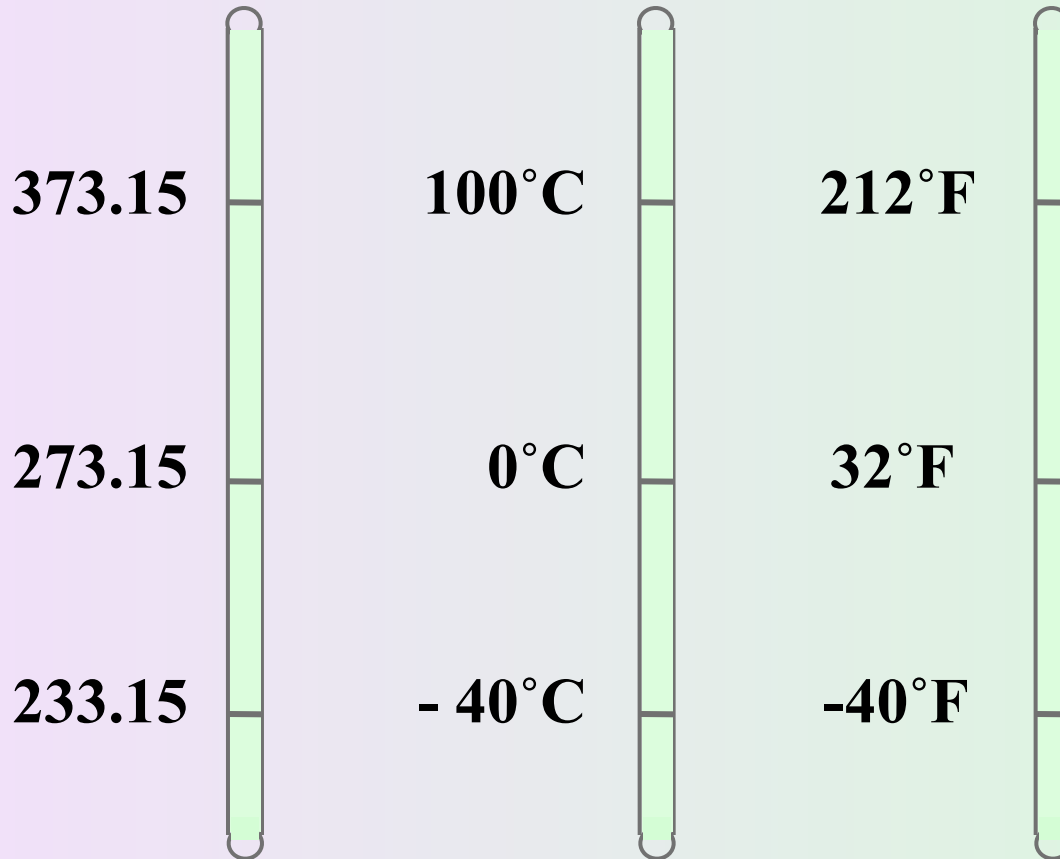
$$\mathbf{C^{\circ} = (F^{\circ} - 32) 5/9}$$

Temperature

Kelvin scale

Celsius scale

Fahrenheit scale



Handling Numbers

In chemistry we deal with very large and very small numbers

Scientific Notation

is a way of dealing with numbers that are either extremely large or extremely small

$$N \times 10^n$$

where **N** is a number between 1 and 10 and **n** is an exponent that can be a positive or negative integer

Exponents

$$100 = 10 \times 10 = 10^2$$

$$0.1 = \frac{1}{10} = 10^{-1}$$

$$0.001 = \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = 10^{-3}$$

Example

Express 568.762 in scientific notation.

$$568.762 = 5.68762 \times 10^2$$

note that the decimal point moved to the left by two places and $n = 2$.

Example

Express 0.00000772 in scientific notation.

$$0.00000772 = 7.72 \times 10^{-6}$$

note that the decimal point moved to the right by six places and $n = -6$.

practice problem 12

Express the following quantities in scientific notation.

$$\text{c. } 4500000.\text{m} = 4.5 \times 10^6$$

↑↑↑↑↑↑↑

$$\text{d. } 6850000000000.\text{m} = 6.85 \times 10^{11}$$

↑↑↑↑↑↑↑↑↑↑↑↑↑↑↑

practice problem 12

Express the following quantities in scientific notation.

e. $0.0054 \text{ kg} = 5.4 \times 10^{-3}$

f. $0.00000687 \text{ kg} = 6.87 \times 10^{-6}$

Scientific Notation

To add or subtract using scientific notation, first write each quantity with the same exponent n . Then add or subtract the N parts of the numbers; the exponent parts remain the same.

practice problem 14e

$$(1.26 \times 10^4 \text{ kg}) + (2.5 \times 10^3 \text{ kg})$$

$$= (1.26 \times 10^4 \text{ kg}) + (0.25 \times 10^4 \text{ kg})$$

$$= 1.51 \times 10^4 \text{ kg}$$

practice problem 14f

$$\begin{aligned} & (7.06 \times 10^{-3} \text{ kg}) + (1.2 \times 10^{-4} \text{ kg}) \\ &= (7.06 \times 10^{-3} \text{ kg}) + (0.12 \times 10^{-3} \text{ kg}) \\ &= 7.18 \times 10^{-3} \text{ kg} \end{aligned}$$

Scientific Notation

To multiply numbers expressed in scientific notation, multiply the N parts of the numbers in the usual way, but add the exponent n 's together.

practice problem 15a - 15b

$$(4 \times 10^2 \text{ cm}) (1 \times 10^8 \text{ cm})$$

$$= 4 \times 10^{10} \text{ cm}^2$$

$$(2 \times 10^{-4} \text{ cm}) (3 \times 10^{-2} \text{ cm})$$

$$= 6 \times 10^{-6} \text{ cm}^2$$

Scientific Notation

To divide numbers expressed in scientific notation, divide the N parts of the numbers in the usual way, but subtract the exponent n 's together.

practice problem 16a - 16c

$$6 \times 10^2 \text{ g} / 1 \times 10^8 \text{ cm}^3$$

$$= 3 \times 10^1 \text{ g/cm}^3$$

$$9 \times 10^5 \text{ g} / 3 \times 10^{-1} \text{ cm}^3$$

$$= 3 \times 10^6 \text{ g/cm}^3$$

The Unit-Factor Method of Solving Problems

also called “dimensional analysis”

it is a good idea to carry units in a calculation to ensure that the answer to the problem has the correct units

The Unit-Factor Method

$$\frac{2.54\text{cm}}{2.54\text{cm}} = \frac{1 \text{ in}}{2.54\text{cm}}$$

dividing both sides of the equation by 2.54cm

$$1 = \frac{1 \text{ in}}{2.54\text{cm}}$$

we create an expression called a unit-factor

$$1 = \frac{2.54\text{cm}}{1 \text{ in}}$$

also called a **conversion factor**

Example

What is the length of a 2.85cm pin in inches?

$$2.85 \text{ cm} \times \frac{1 \text{ in}}{2.54 \text{ cm}} = 1.12 \text{ in}$$

practice problem 17a

convert 360 s to ms

$$360 \cancel{\text{s}} \times \frac{1000 \text{ ms}}{1 \cancel{\text{s}}} = 3.6 \times 10^5 \text{ ms}$$

practice problem 17b

convert 4800 g to kg

$$4800\cancel{\text{g}} \times \frac{1 \text{ kg}}{1000\cancel{\text{g}}} = 4.8 \text{ kg}$$

Example 2 - 4

what is a speed of 550 meters per second in kilometers per minute

$$\frac{550 \cancel{\text{ m}}}{1 \cancel{\text{ s}}} \times \frac{1 \text{ km}}{1000 \cancel{\text{ m}}} \times \frac{60 \cancel{\text{ s}}}{1 \text{ min}}$$

= $\frac{33 \text{ km}}{1 \text{ min}}$

practice problem 19

How many seconds are there in 24 hours ?

$$24 \text{ hr} \times \frac{60 \text{ min}}{1 \text{ hr}} \times \frac{60 \text{ s}}{1 \text{ min}} = 8.64 \times 10^4 \text{ s}$$

practice problem 20

the density of gold is 19.3 g/mL. What is the gold's density in decigrams per liter ?

$$\frac{19.3 \cancel{\text{g}}}{1 \cancel{\text{mL}}} \times \frac{0.1 \text{ dg}}{1 \cancel{\text{g}}} \times \frac{1000 \cancel{\text{mL}}}{1 \text{ L}}$$

= $\frac{1930 \text{ dg}}{1 \text{ L}}$

Example

Where were you a billion seconds ago ?

$$1 \times 10^9 \text{ sec} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{1 \text{ hour}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ hours}} \times \frac{1 \text{ year}}{365 \text{ days}} = 31.7 \text{ years}$$